## MATH 2551, Spring 2018 Practice Exam 2, Chapter 14

Guideline: Please read the following carefully.

Remember to show all your work; including all intermediate steps and also explain in words how you are solving a problem. Partial credits are available for most problems. One side of a letter sized sheet of paper for formula. Calculator is not allowed in this exam. You have 50 minutes.

Problem 1. Calculations.

(a) Find the directional derivative of f(x, y, z) = xy + yz + zx at P(1, -1, 1)in the direction of  $\mathbf{i} + 2\mathbf{j} + \mathbf{k}$ 

(b) Find the rate of change of  $f(x, y) = xe^y + ye^{-x}$  along the curve  $\mathbf{r}(t) = (lnt)\mathbf{i} + t(lnt)\mathbf{j}$ .

(c) Find  $\frac{\partial u}{\partial s}$  for  $u = x^2 - xy$ , x = scost, y = tsins.

(d) Find the value of  $\frac{dy}{dx}$  if  $x\cos(xy) + y\cos(x) = 2$  at the point (0, 2).

(e) For  $f(x,y) = \frac{x^2 - y^4}{x^3 - y^4}$ , determine whether or not f has a limit at (1,1).

**Problem 2** Consider the function  $f(x, y, z) = \sqrt{x} + \sqrt{y} + \sqrt{z}$ .

(a) Find the equation for the tangent plane to the level surface f = 4 at the point P(1, 4, 1).

- (b) Find the equation for the normal line to f = 4 at P(1, 4, 1).
- (c) Use differentials to estimate f(0.9, 4.1, 1.1).

**Problem 3**. Find the area of the largest rectangle with edges parallel to the coordinate axes that can be inscribed in the ellipse  $\frac{x^2}{9} + \frac{y^2}{4} = 1$ .

**Problem 4** Find the absolute extreme values taken on  $f(x, y) = \frac{-2y}{x^2+y^2+1}$  on

the set  $D = \{(x, y) : x^2 + y^2 \le 4\}.$